**Thesis Proposal**

The Effect of Individual Study Power on the Performance of Bayesian Evidence Synthesis in the Context of Multiple Regression Analysis

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# Introduction

Much focus has been given to the necessity to accumulate evidence across replications in order to gain certainty about the presence of an effect and its size. To this end, meta-analysis and Bayesian Sequential Updating (BSU; [Schönbrodt, Wagenmakers, Zehetleitner, and Perugini](#_CTVL001ea319636f18042e9bb984c4449a9dcd2), [2016](#_CTVL001ea319636f18042e9bb984c4449a9dcd2)) are among the available tools that can be used. However, both are problematic when aggregating effects over conceptual replications, i.e., studies that investigate the same effect but differ in design, operationalization of the dependent variable, or measurement of the variables [(Klugkist & Volker, 2022)](#_CTVL001ed20edd2d9fa4b3c95e9a8c15908e1b4). An alternative tool that could tackle this problem is Bayesian Evidence Synthesis (BES; [Kuiper, Buskens, Raub, and Hoijtink](#_CTVL001cfeaa701f1b0457e89f5516ec8480e60), [2013](#_CTVL001cfeaa701f1b0457e89f5516ec8480e60)). Instead of pooling effect sizes or data, BES aggregates evidence at the level of hypothesis. That is, a Bayes factor (BF; [Kass and Raftery](#_CTVL001a9d2bff361364567854b4558298835d8), [1995](#_CTVL001a9d2bff361364567854b4558298835d8)) is used to quantify the relative support for one hypothesis over another in each study and BES aggregates the BFs to quantify the overall support across all studies. However, the performance of BES has not been thoroughly investigated in realistic situations when the studies in the set have different evidential value, i.e., when some of them are underpowered, while others are highly powered.

Previous research has shown that BES performs very well if all included studies have adequate power [(Klugkist & Volker, 2022](#_CTVL001ed20edd2d9fa4b3c95e9a8c15908e1b4)[; van Wonderen, 2022](#_CTVL001b770535181964a8385f2f95881dc39a9)[; Volker, 2022)](#_CTVL001b8adcb738da14878a197115fc60af73c). However, there is evidence that that even a single underpowered study with small sample size can strongly reduce the support for the true hypothesis [(Volker, 2022)](#_CTVL001b8adcb738da14878a197115fc60af73c). Another study, however, showed that this effect diminished when the set of studies was larger and included more studies with adequate sample size [(van Wonderen, 2022)](#_CTVL001b770535181964a8385f2f95881dc39a9). Another finding was that if the set of studies included only studies with small samples, the support *against* the true hypothesis accumulated [(Volker, 2022)](#_CTVL001b8adcb738da14878a197115fc60af73c).

In a set of conceptual replications power can differ across studies not only because of the sample size but also because of other factors, such as the scale of the outcome and the analysis type (e.g., logistic, probit, linear regression,), or the complexity of the hypothesis, that is, the number of constraints imposed on the parameters [(Klugkist & Volker, 2022](#_CTVL001ed20edd2d9fa4b3c95e9a8c15908e1b4)[; Volker, 2022)](#_CTVL001b8adcb738da14878a197115fc60af73c). Thus, it is important first to adequately quantify the power of each study while taking all these factors into account. Only then can the effect of individual study power on the performance of BES be systematically evaluated.

Using such power quantification this paper aims to (1) elucidate how the distribution of power in the study set relates to the performance of BES, and in particular, to what extent can highly powered studies compensate for underpowered ones; (2) provide applied researchers with R code to calculate power for individual studies; and (3) provide power tables that can give impression of how reliable the aggregate support from BES would be, given certain study and population characteristics.

# Analytical Strategy

To address these aims simulation studies will be performed, in which a study set is simulated such that data for individual studies is generated and analyzed according to multivariate linear, logistic or probit regression. The following aspects will be manipulated across simulation studies: the number of the studies in set; the distribution of individual study power in the study set; the number of the predictors in the regression model, as well as population characteristics such as effect size and correlation between the predictors. All analyses will be performed in R (version 4.2.0; [R Core Team](#_CTVL0010912ec558aba48929938a70d2cdbc8e5), [2022](#_CTVL0010912ec558aba48929938a70d2cdbc8e5))

Approximate adjusted fractional Bayes factor [(Gu, Mulder, & Hoijtink, 2018)](#_CTVL0018631fa27fff94c1195d6b47a65820f60) will be computed with the R package BFpack, version 1.0.0 [(Mulder et al., 2019)](#_CTVL001da9a1c4f82bc4a588210efb73f93995f). The performance of BES will be evaluated as the proportion of times the BES-aggregate shows sufficient support for the true hypothesis across iterations. Different definitions of sufficient support will be investigated.

In this paper the power of a study to test one hypothesis Hi against an alternative hypothesis Ha is defined and quantified as the probability of obtaining a BF that supports Hi (i.e., BF>1) if Hi is true and the probability of obtaining a BF that supports Ha (i.e., BF<1) if the Ha is true. This definition has been adapted from the concept of reliability of a BF [(Hoijtink, 2011)](#_CTVL0016b128cb6bb4b4fbe8f2e06410e3e3162) that has also been employed in [Fu](#_CTVL00147811da3db5d4db8968434409b7fcf60)’s [(2022)](#_CTVL00147811da3db5d4db8968434409b7fcf60) algorithm for sample size determination for Bayesian hypothesis testing.

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